

T-61.6040 Assignment-06/2011

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AIM

Implementation of bayesian kernel methods for regression algorithm discussed in the lecture using gaussian for a motorcycle dataset.

$$k_{GAU} = (x_i, x_j) = \exp(-\|x_i x_j\|_2^2 / s^2), \text{ and } s = \{0.4, 0.8, 1.6\}, \text{ and } A = \{1, 2, 4\}. \quad (1)$$

Datasets

Motorcycle dataset for regression analysis.

Implementation

Load and zscore normalize the X and sort X and Y values. Zscore normalization can also be done using the method described in the lecture.

```
X1 = zscore(dlmread('motorcycle_X.txt'));  
Y = dlmread('motorcycle_y.txt');  
[X idx] = sort(X1); Y = Y(idx);
```

Calculate Gaussian kernel function.

```
K = exp(-pdist2(X,X).^2/S(i).^2);
```

Find the inverse and calculate the alpha values

```
[M ,N] = size(K);  
KC = (K + a(j)^2 .* eye(N, N)) \ eye(N, N);  
alpha = KC*Y;
```

Generate uniform distribution of values and calculate the variance

```

X_s = linspace(-2, 2.5, 200)';
K_s = exp(-pdist2(X, X_s).^2/S(k).^2);
for iter = 1:200
temp1(iter) = a(j).^2-(K_s(:, iter)')*KC*K_s(:, iter));
end
variance = temp1' + diag((exp(-pdist2(X_s, X_s).^2/S(k).^2)));

Calculate the mean
meen = K_s'*alpha;

Plot the mean and standard deviations on the data
fh(Count) = scatter(X,Y);
hold on
plot(X_s, meen, 'k--')
hold on
plot(X_s, meen+3*sqrt(variance), 'r--');
hold on
plot(X_s, meen-3*sqrt(variance), 'r--');

save the plots
title(['A =', num2str(a(j)) , ' S = ', num2str(S(k))]);
%—print figure —
fnout = ['Count=', num2str(Count, '%.2d'), '.jpg'];
print('-djpeg', '-r150', fnout);
clf;

```

The Gaussian kernel implementation is carried out for all the values of $s = \{0.4, 0.8, 1.6\}$, and $A = \{1, 2, 4\}$. for dataset and these plots are shown in figure 1, 2 and 3 respectively.

Running of code for Gaussian kernel in matlab are 'guass'.

Results

Figure 3 showing the Gaussian process algorithm on motorcycle data tending towards a linear fit.

References

- [1] Lecture slides and course book.

Attachments

Matlab code guass.m and datasets have been archived along with this report.

Figure 1: Gaussian process algorithm on motorcycle data.

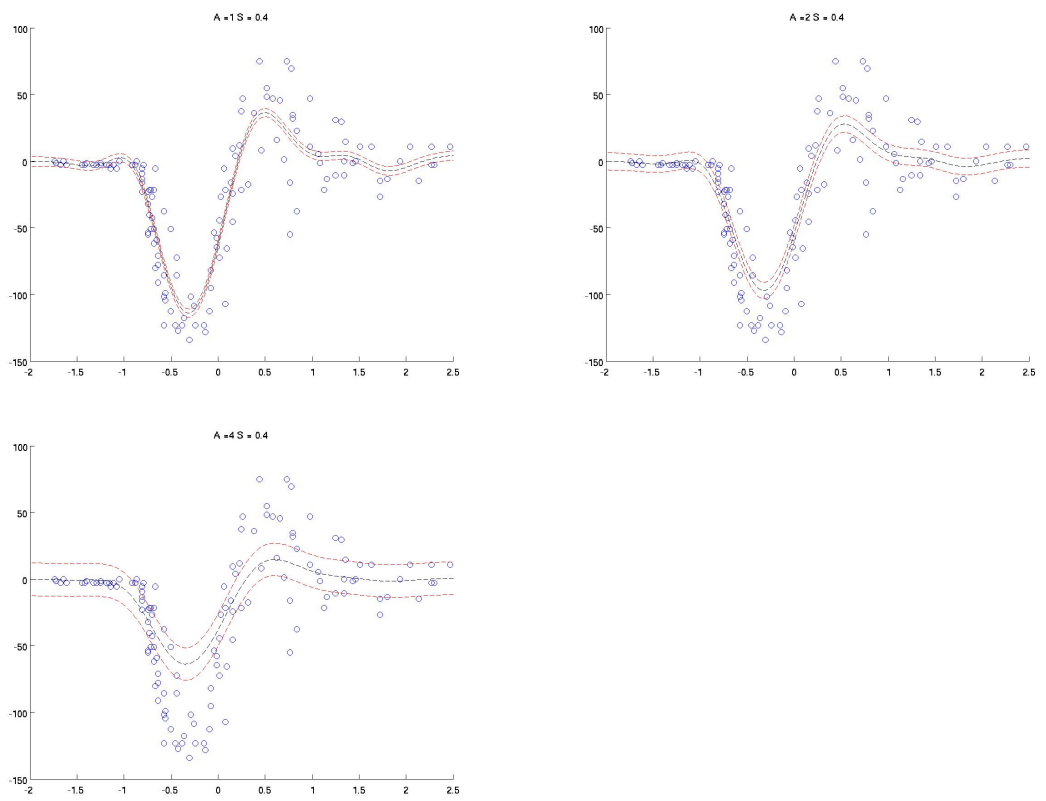


Figure 2: Gaussian process algorithm on motorcycle data.

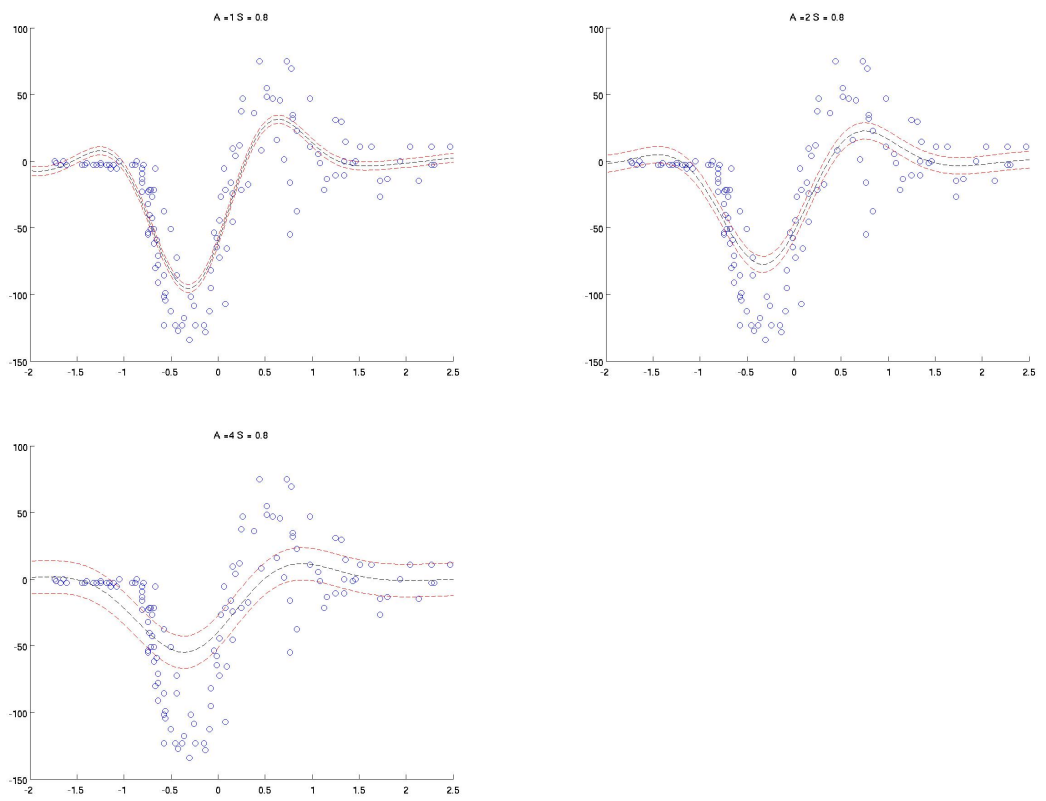


Figure 3: Gaussian process algorithm on motorcycle data.

